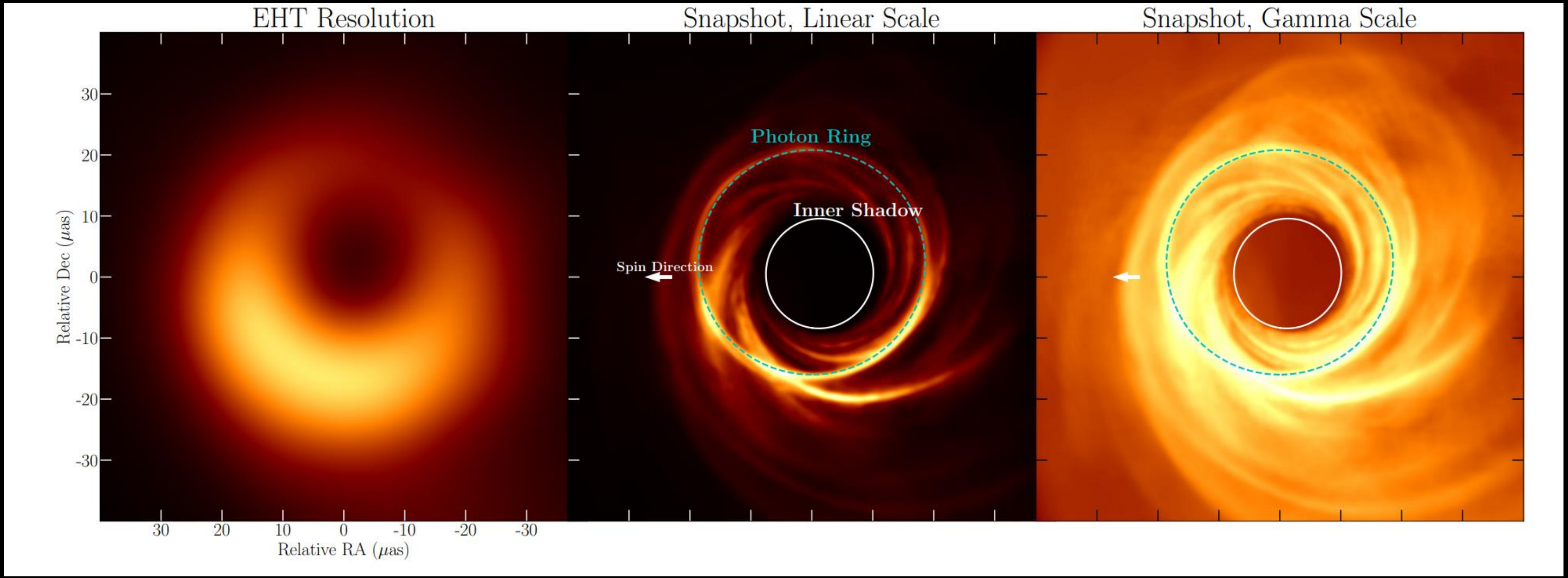
The inner shadow of a black hole:
A direct view of the event horizon

arXiv: 2106.00683



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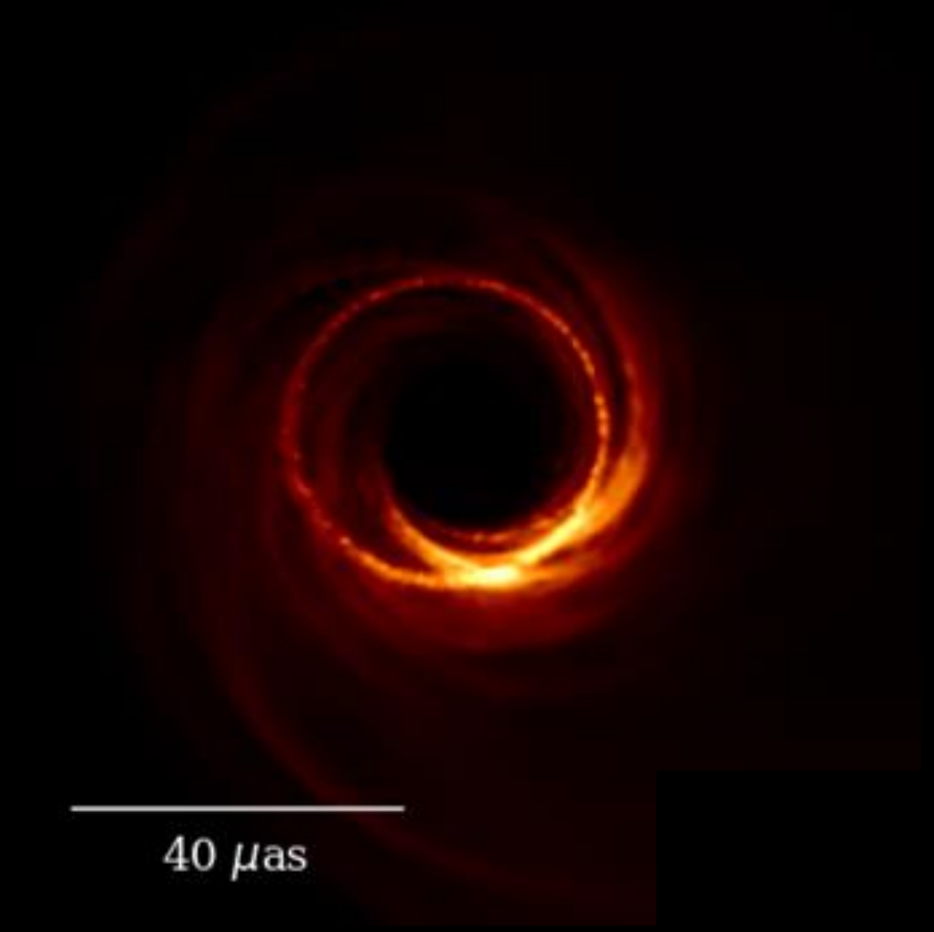
NHFP
NASA Hubble Fellowship Program

PRINCETON UNIVERSITY

Event Horizon Telescope

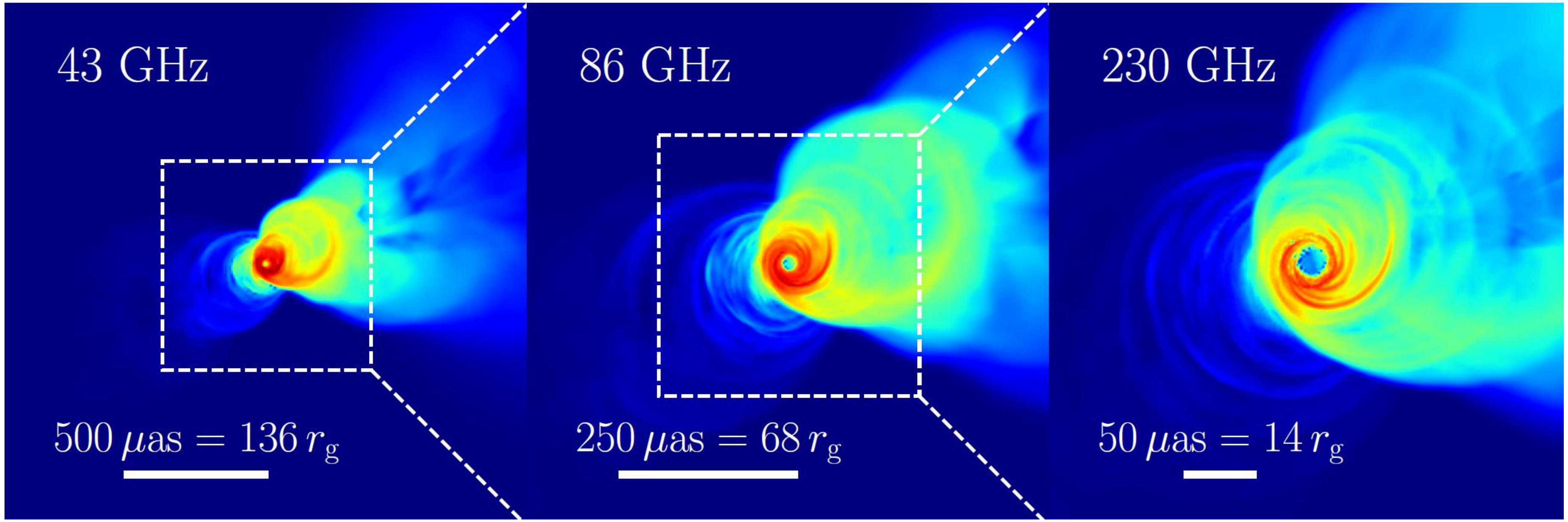
What happens when we look at GRMHD simulation images at high dynamic range?



Simulations in this talk are of **magnetically arrested disks (MADs)**

From Chael+ 2019 using KORAL code (Sadowski+ 2013,16)

What happens when we look at GRMHD simulation images at high dynamic range?



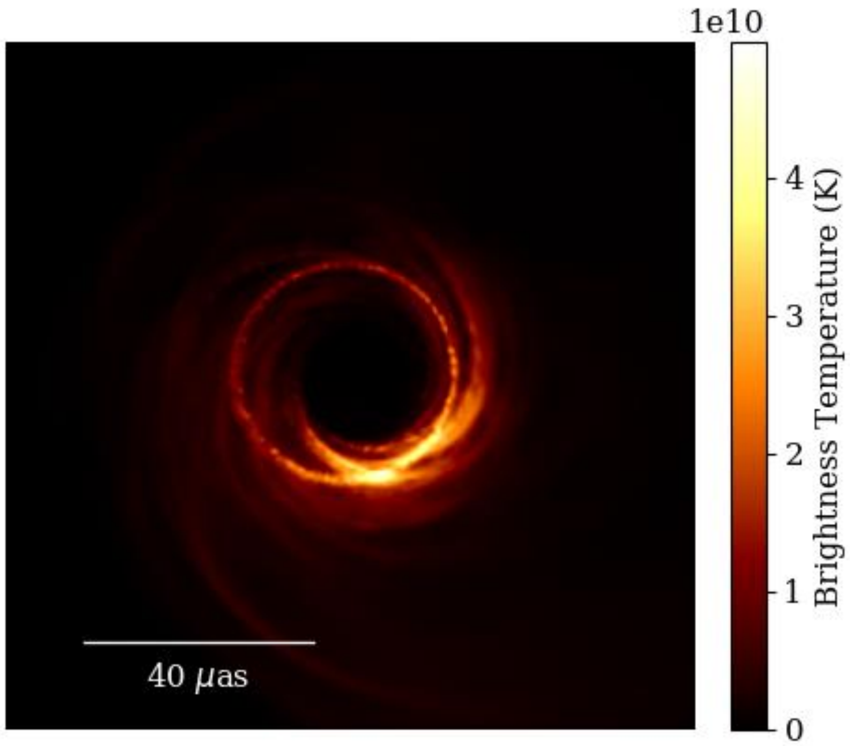
- If the simulation is run long enough and with the right prescription for electron heating, we see a visible jet like in M87
- Future EHT observations should be able to see this dim extended jet emission around the black hole image

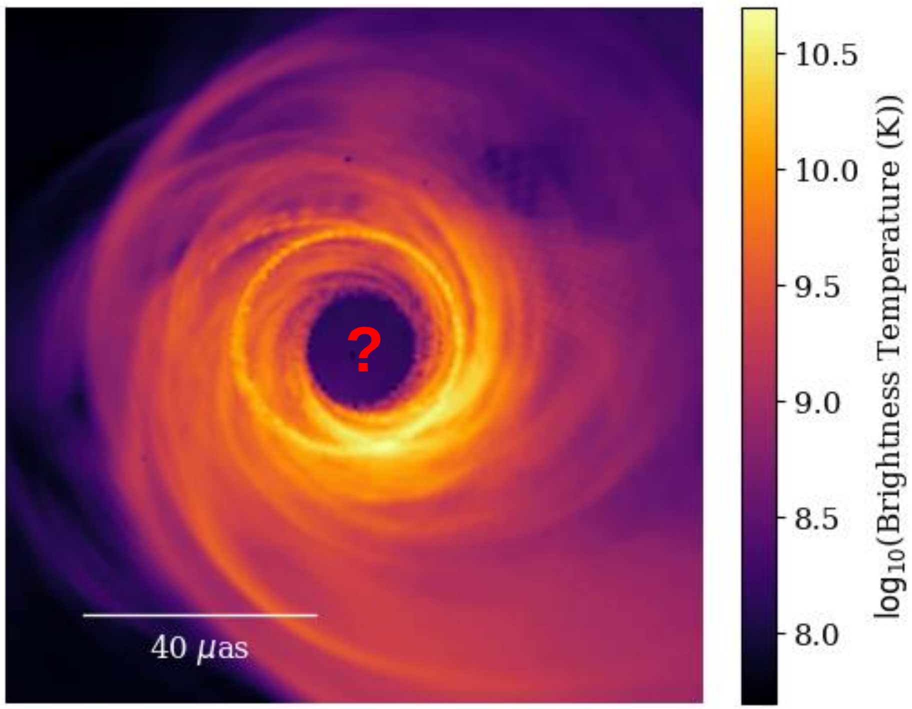
Simulations in this talk are of **magnetically arrested disks (MADs)**

From Chael+ 2019 using KORAL code (Sadowski+ 2013,16)

Image Credit: Chael+ 2019

A sharp central brightness depression in high dynamic range images



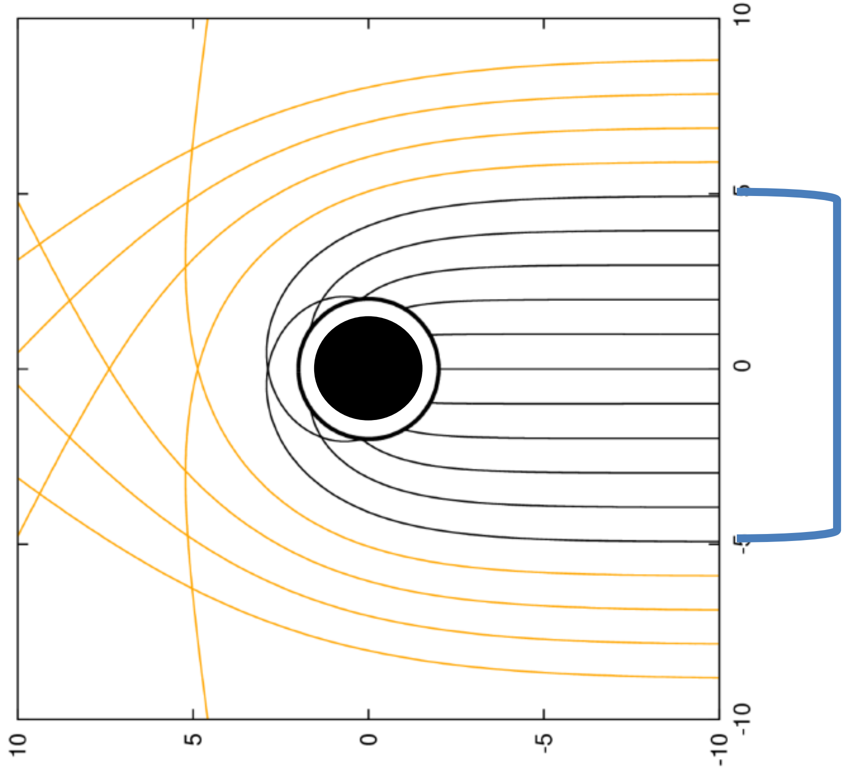


Is this a consequence of jet sigma cut? An artifact of polar coordinates?

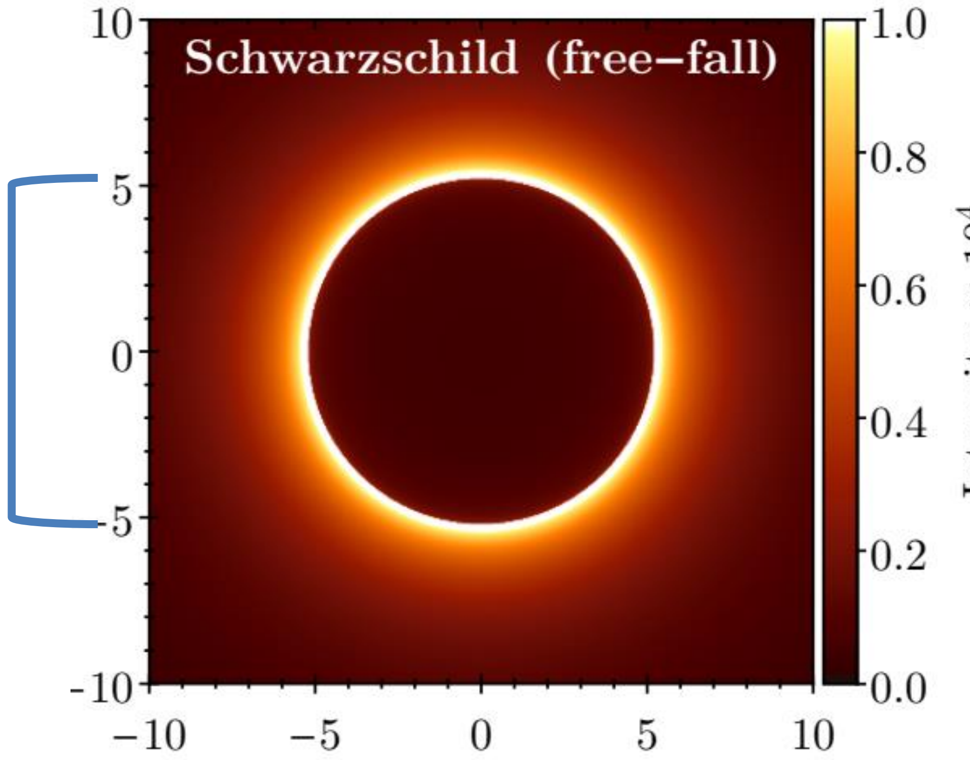
Sharp central brightness depression in GRMHD images

- This is **the inner shadow**: the lensed (n=0) image of the equatorial event horizon.
- While not ‘universal’ like the photon ring, **many GRMHD simulations have the conditions necessary to make this feature observable**
- Features of this image (radius, eccentricity, offset from the photon ring) **can be used to measure spin and inclination**
- The **ngEHT will have the dynamic range and resolution necessary** to observe this feature

The Critical Curve or “Black Hole Shadow”



$$d_{\mathrm{shadow}} = 2\sqrt{27}GM/c^2$$



- The ‘critical curve’ on the image separates of rays that end on the event horizon with those that escape to infinity
- The interior of the critical curve is the ‘black hole shadow’, where all rays end on the horizon
- The shadow is particularly prominent as an image feature when the emission is optically thin and **spherically symmetric**

Image credit: Keiichi Asada
Narayan+ 2019 (also Falcke+ 2000, many others)

Lensed images of the equatorial plane

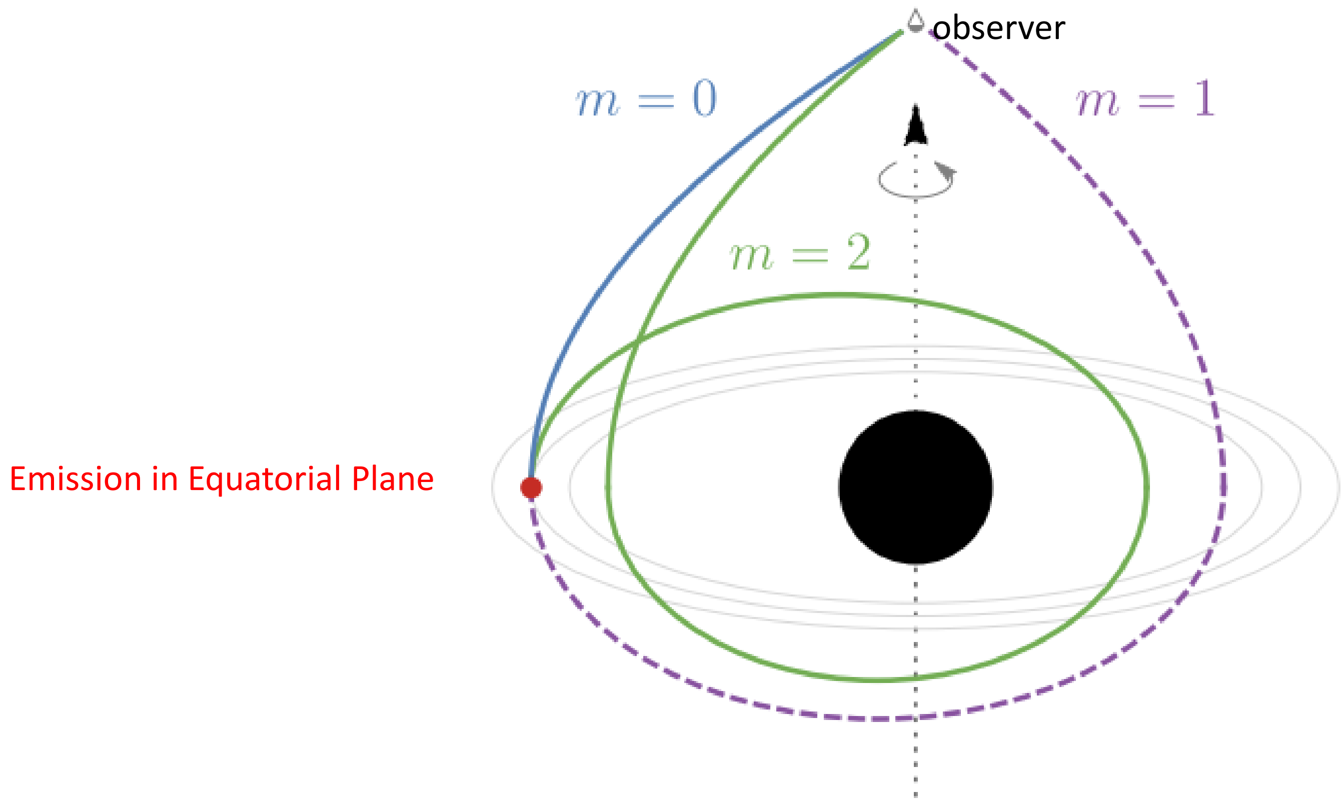
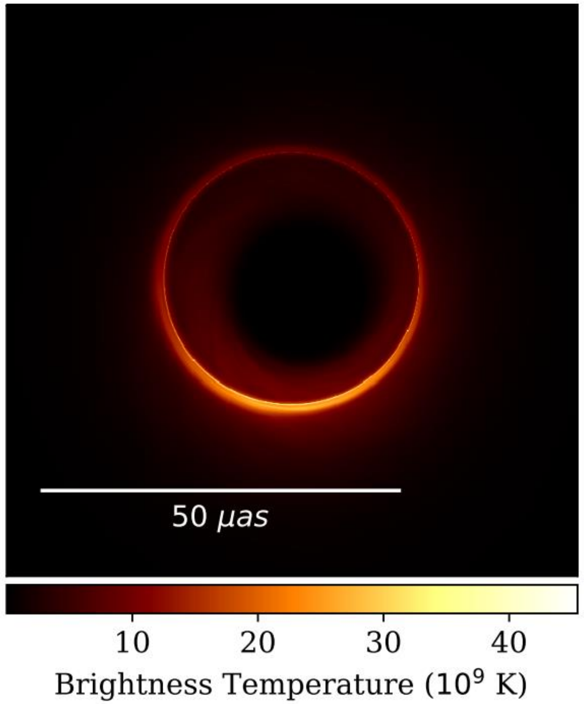


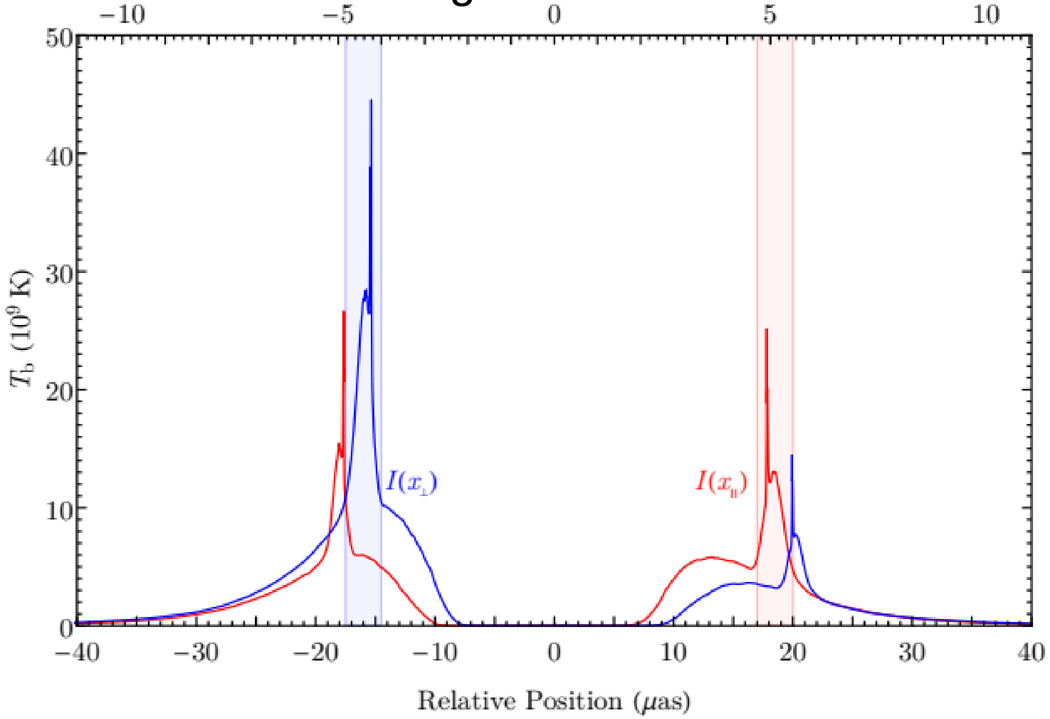
Image credit: Gralla & Lupsasca 2019

Photon Rings

Time-averaged GRMHD



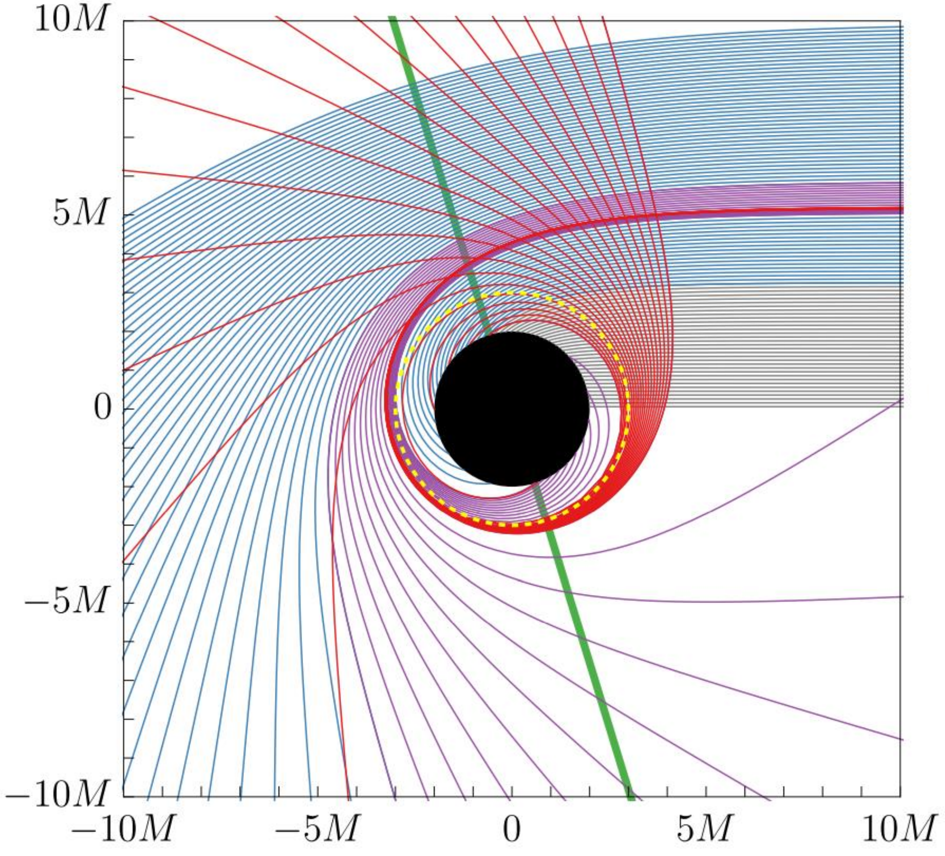
Angular slices

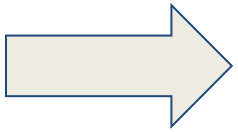


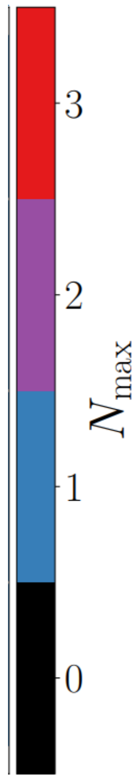
- As geodesics wrap around the black hole multiple times, they form a **series of images** lensed into **increasingly narrow rings**
- These subrings approach the critical curve exponentially.
- Resolving the subrings requires a **spatially limited emission region** (e.g. emission confined to the equatorial plane)
- See Alex's talk from Monday!

Image credit: Johnson+ 2019
Simulation Credit: George Wong

Lensed images of the equatorial plane







This feature has been discussed many times in analytic models in e.g.:

- Luminet 1979, Figure 2
- Takahashi 2004, Figure 1
- Gralla, Holz, Ward 2019, Figure 1
- Dokuchaev 2019

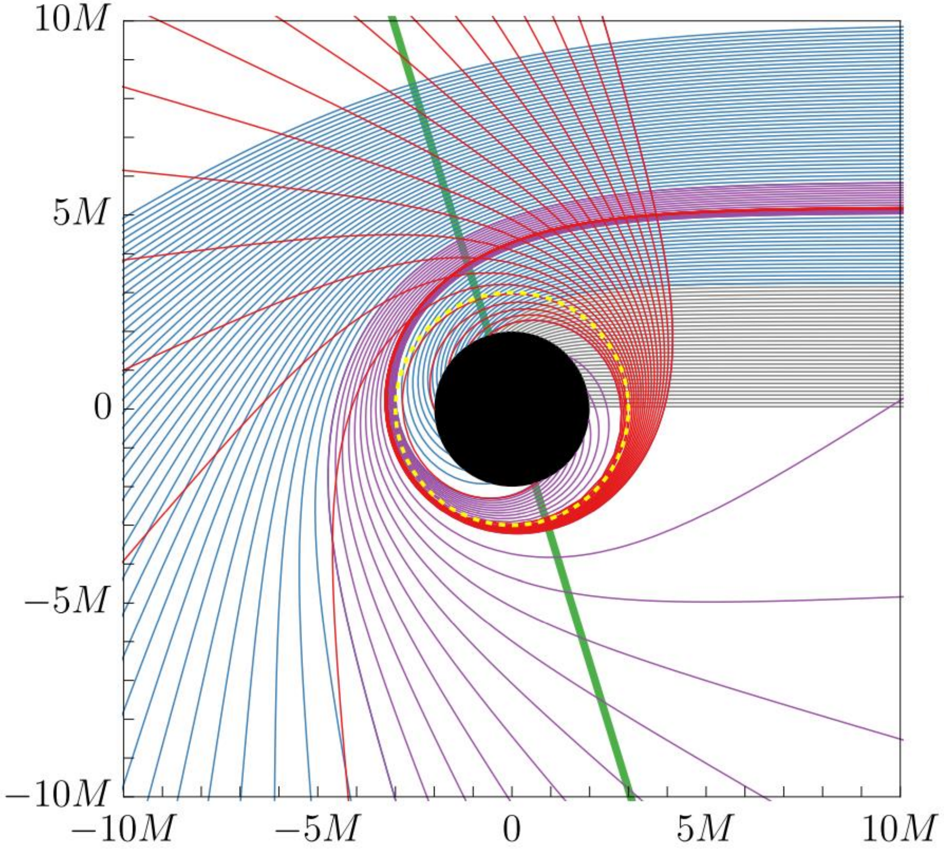
Image credit Chael+ 2021

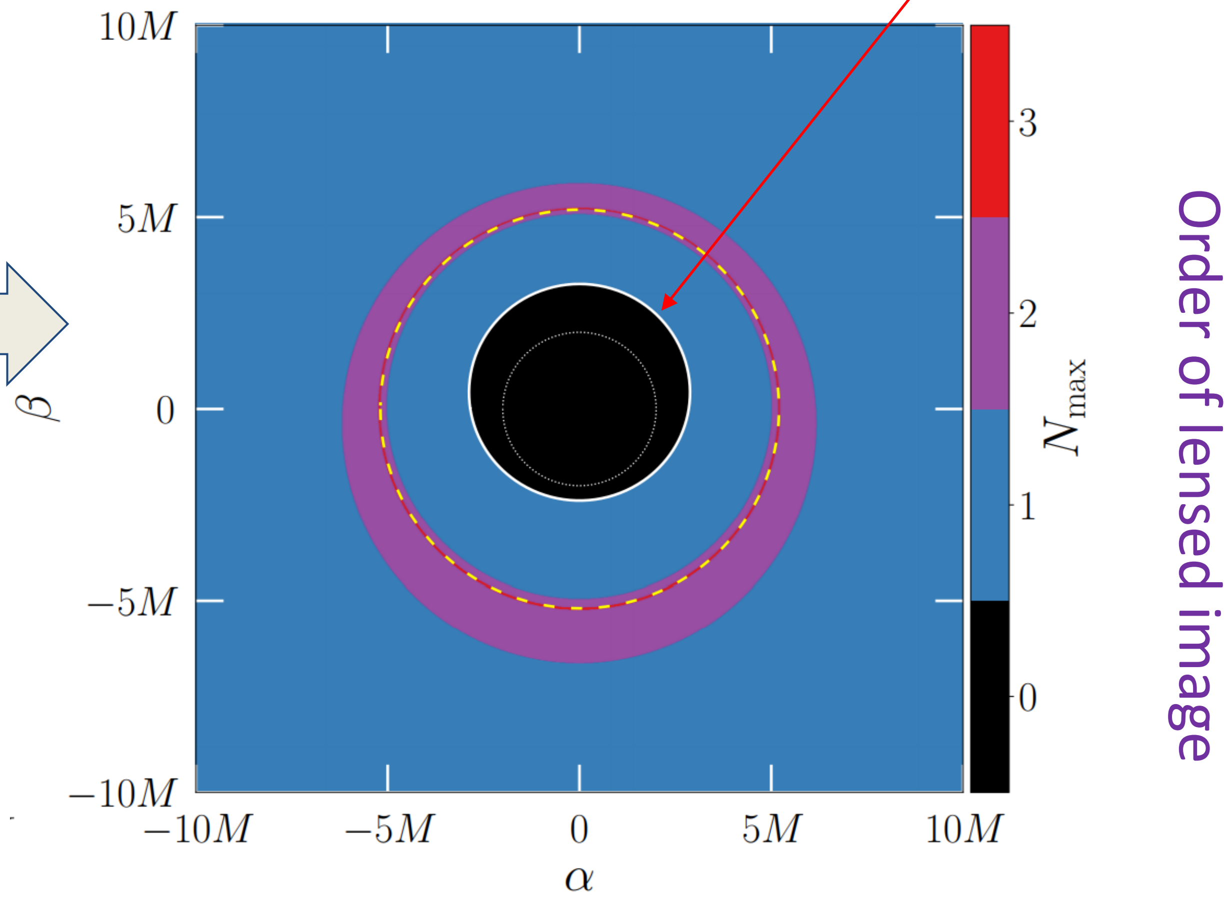
Lensed images of the equatorial plane

Curve: n=0 image of the equatorial event horizon

Interior: Silhouette of the horizon northern hemisphere

Multiply-lensed images of the equatorial plane





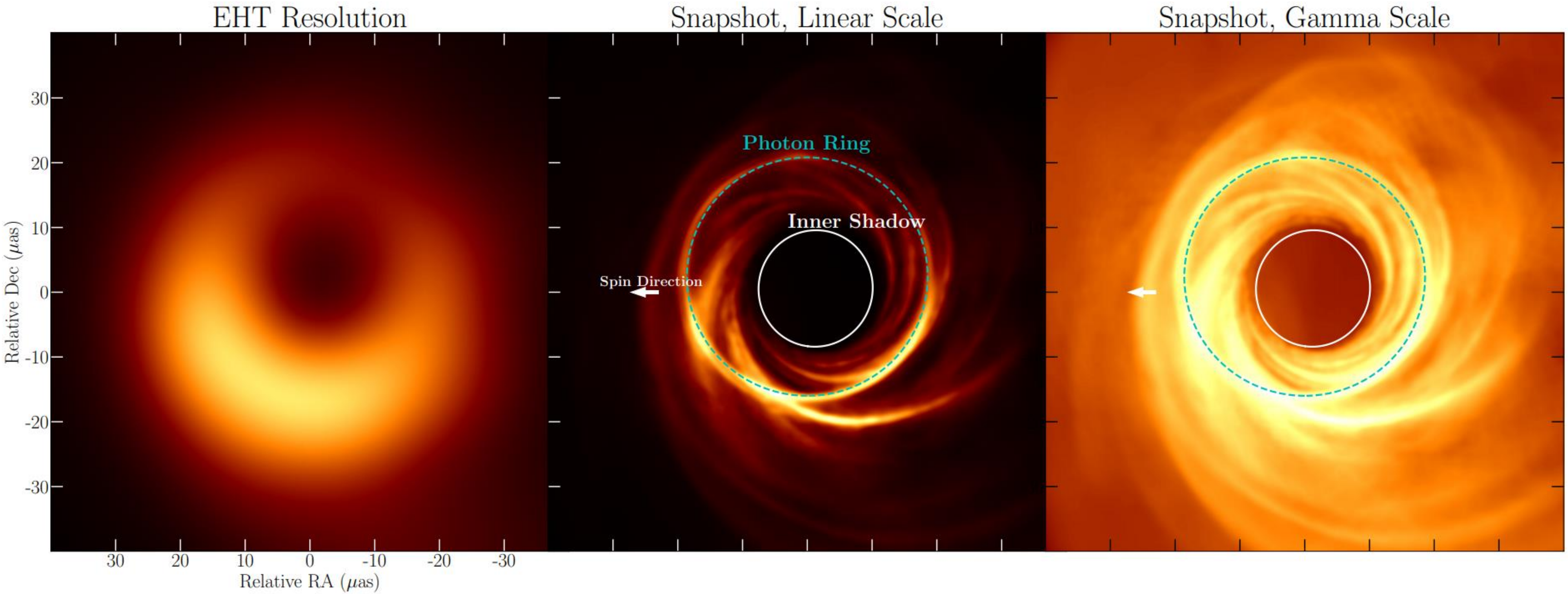
(a=0, i=17 deg)

This feature has been discussed many times in analytic models in e.g.:

- Luminet 1979, Figure 2
- Takahashi 2004, Figure 1
- Gralla, Holz, Ward 2019, Figure 1
- Dokuchaev 2019

Image credit Chael+ 2021

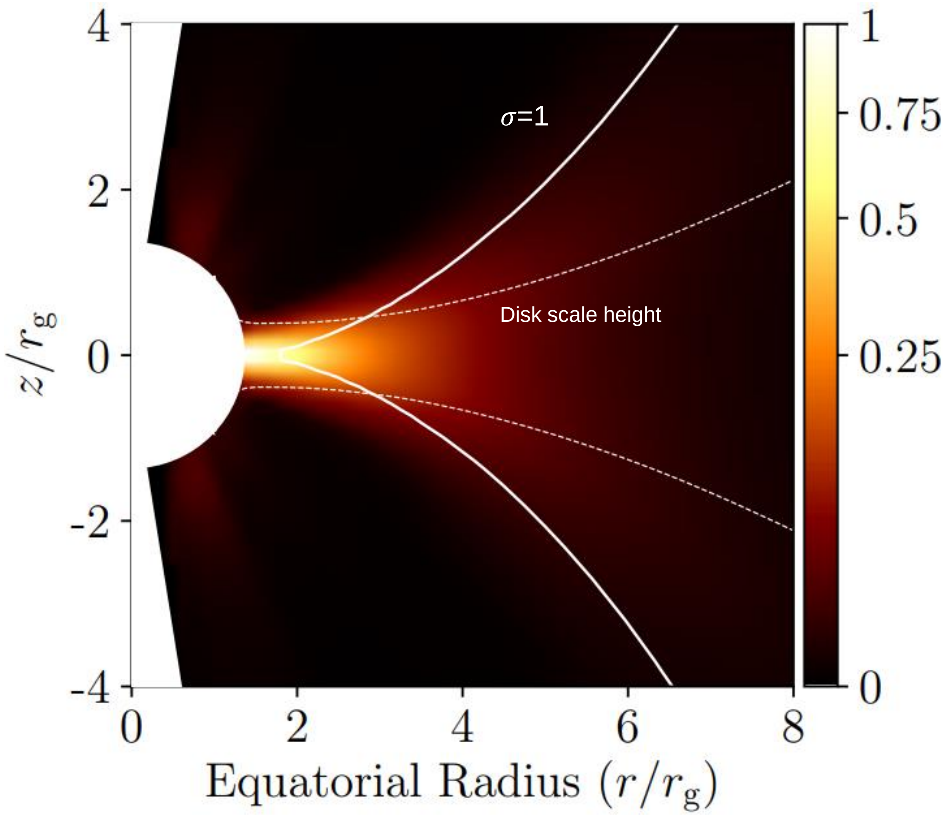
Inner shadow in GRMHD images

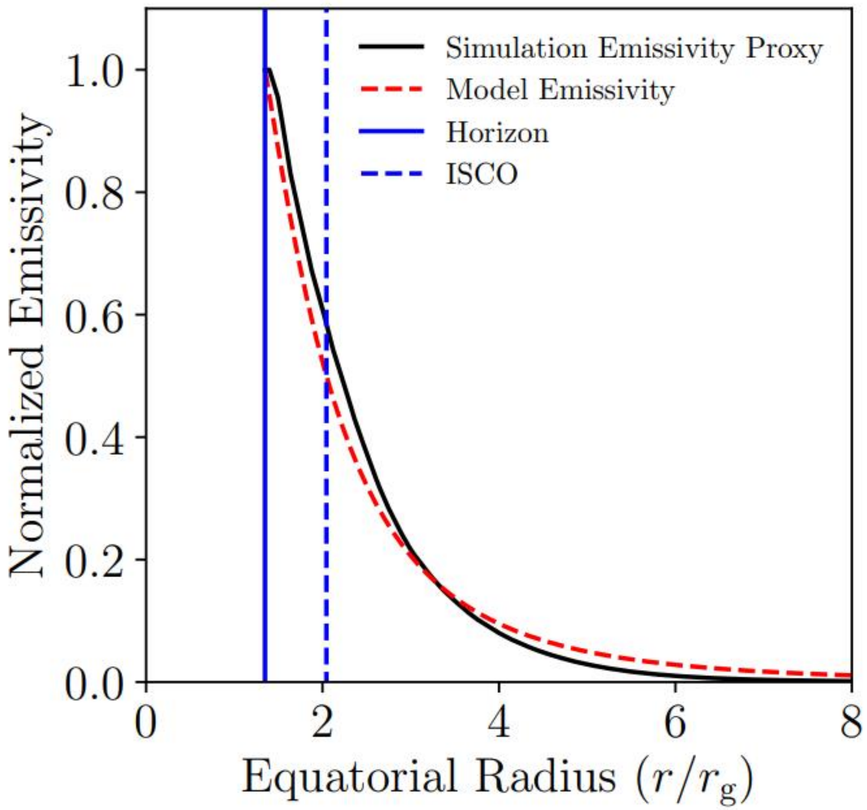


- This high dynamic range feature is the **outline of the equatorial event horizon**
- While not 'universal' like the shadow/photon ring, it may be visible with the ngEHT

Why is the horizon visible in these simulations?

Emissivity proxy (same as in Porth+ 2019)

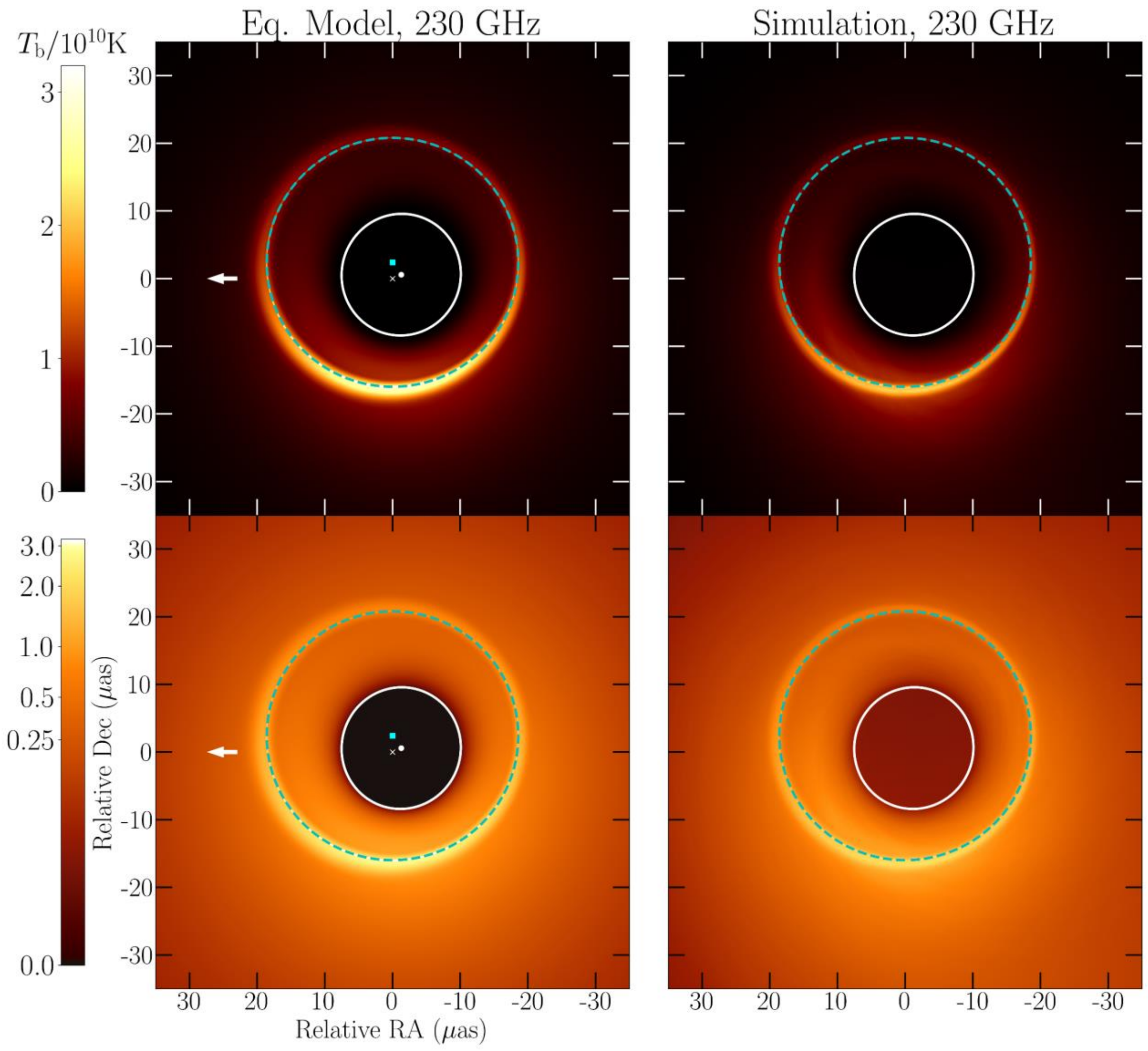




Equatorial slice

- The 230 GHz emissivity is predominantly **equatorial** in this simulation
- It does not truncate at the ISCO, but **extends to the horizon**
- Fluid velocities are **subkeplerian** – reducing the overall redshift

Time-averaged simulation images at high dynamic range

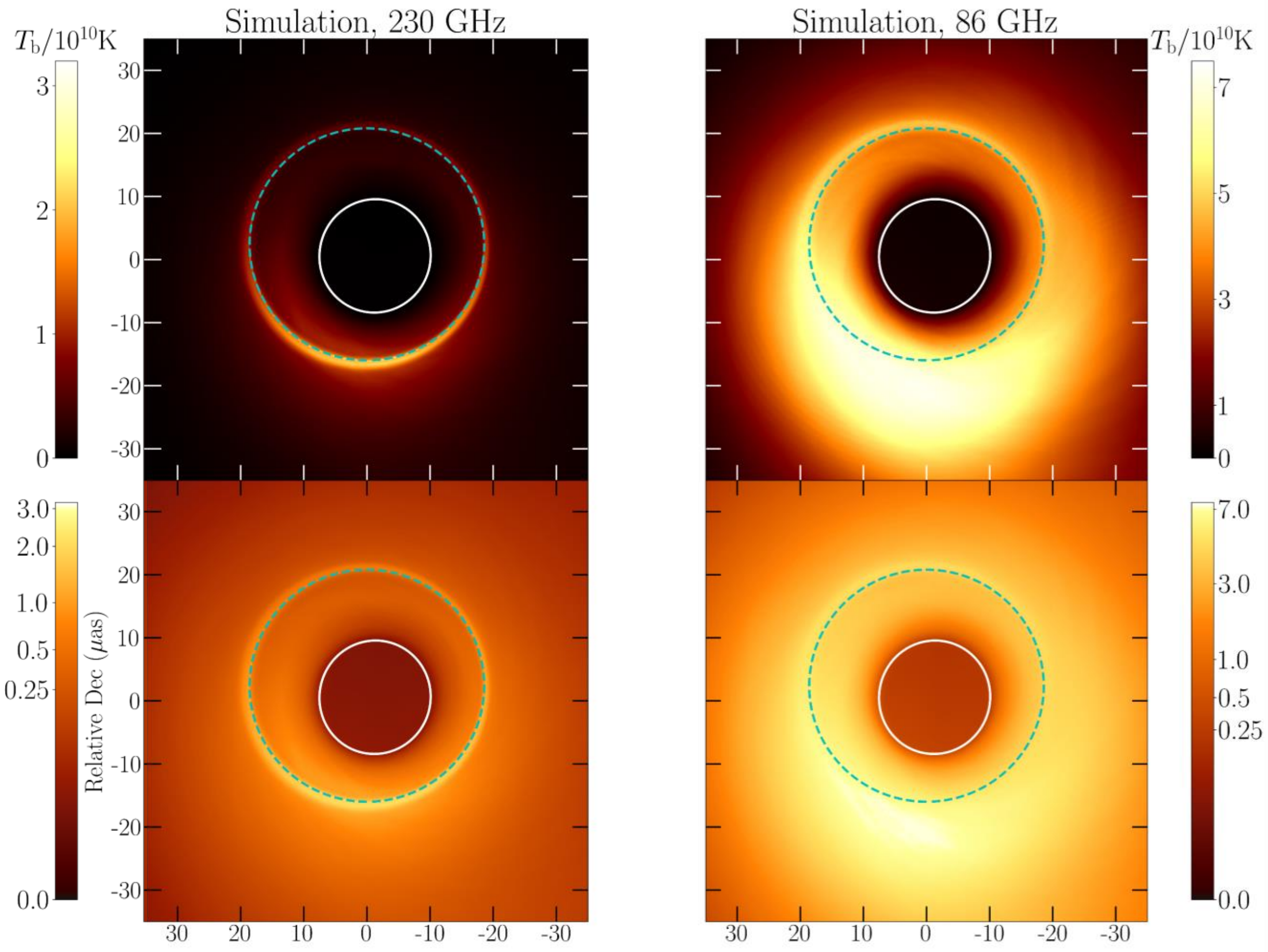


- The averaged simulation image shares the **primary features of an image from a purely equatorial disk model** (Gralla,Lupsasca,Marrone+ 2020)
- **Forward jet emission** in the simulation gives the horizon image a finite "floor"

230 vs 86 GHz Simulation images

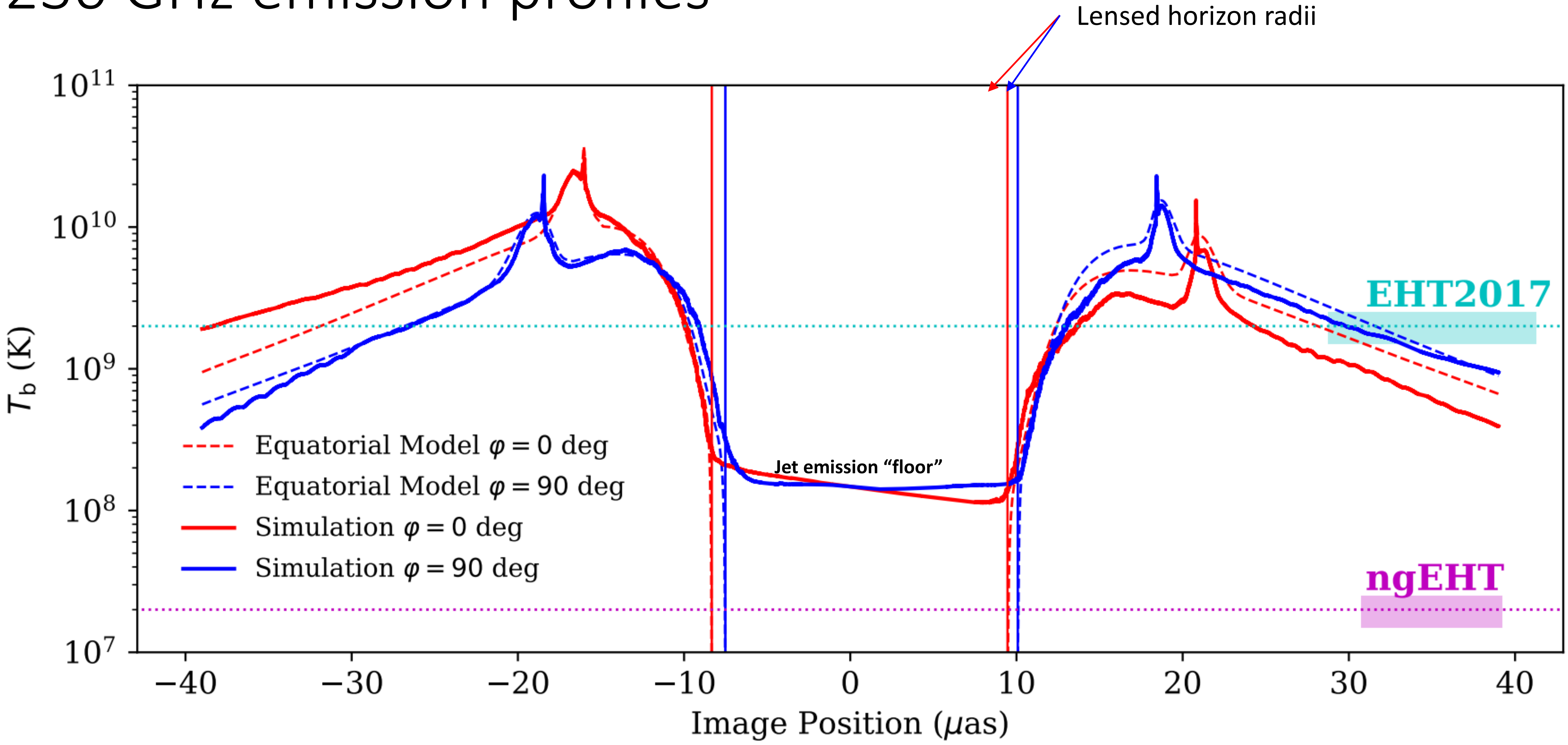
Linear scale

Gamma scale



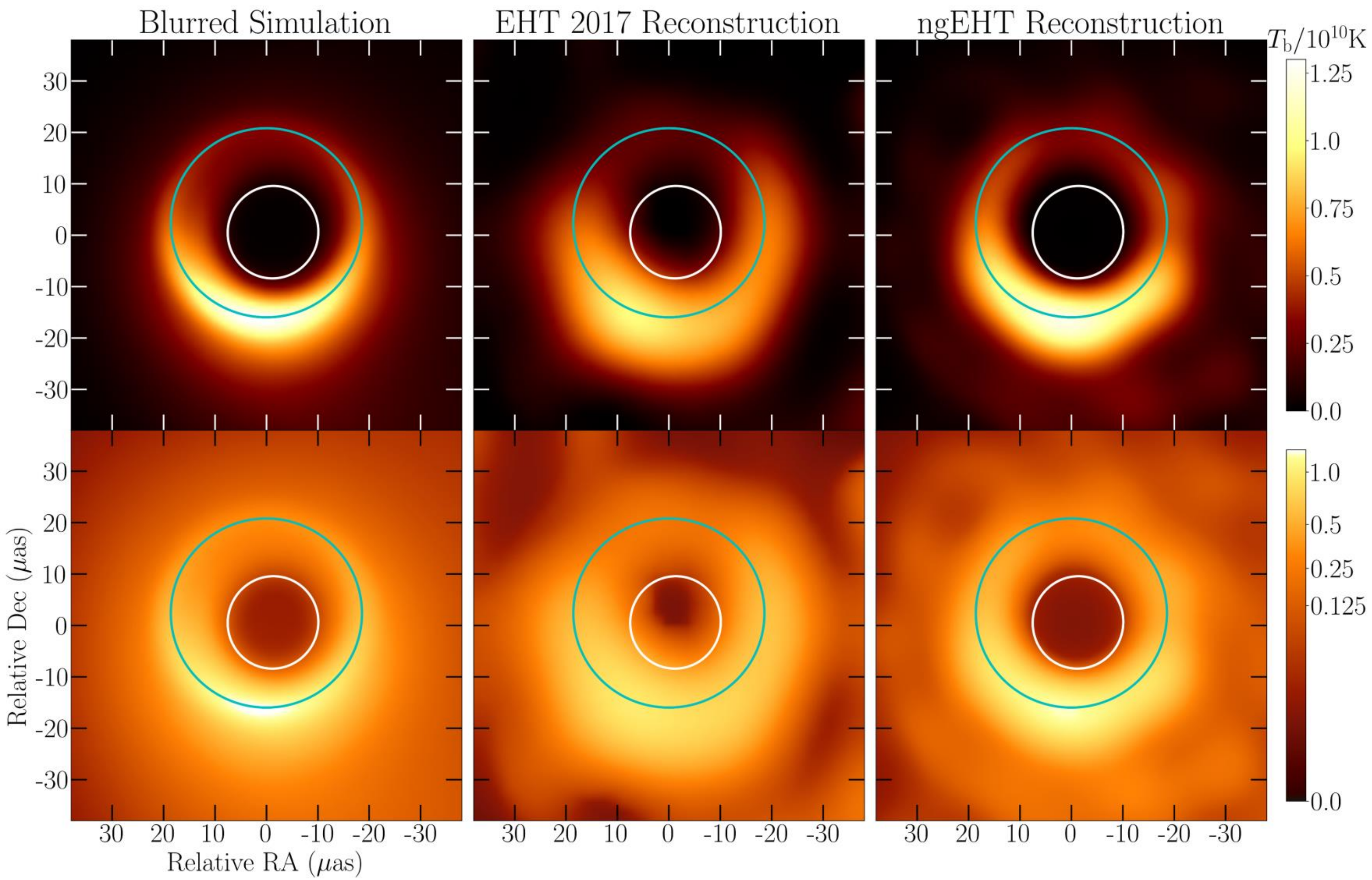
- The *n*=1 photon ring is supressed by optical depth at 86 GHz, but the *n*=0 lensed horizon image is not
- Optical depth doesn't matter if the emission is primarily equatorial and not obscured by the forward jet

230 GHz emission profiles



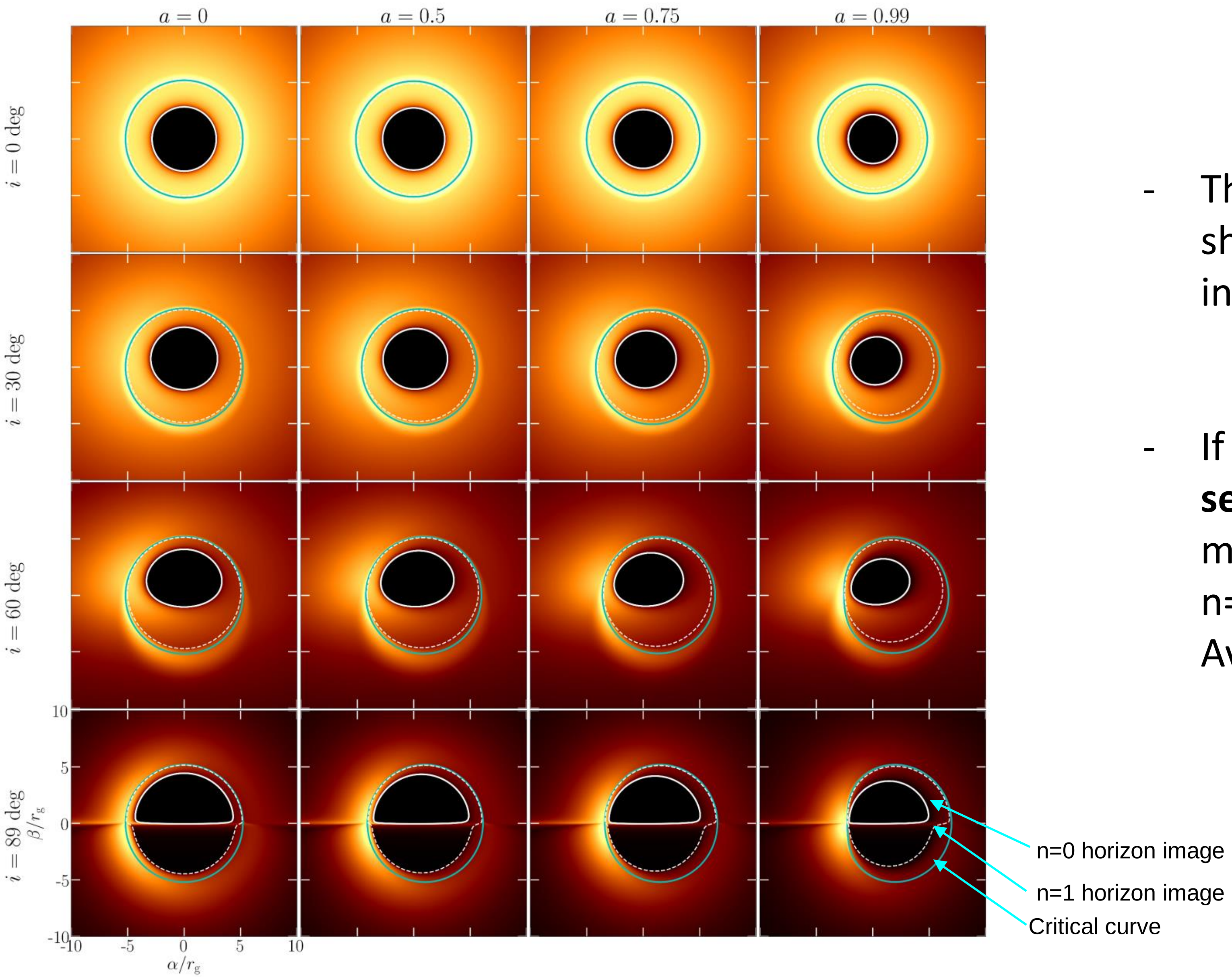
The ngEHT should have the dynamic range to observe the inner shadow feature, if present

EHT 2017 and ngEHT image reconstructions



- 'Realistic' EHT imaging scripts using closure phases and amplitudes, but on the time-averaged image
- **Imaging algorithms can detect the inner shadow in ngEHT data** – analytic modeling may constrain its shape more precisely

Inner shadow images provide another probe of spacetime



- The horizon image changes in shape and size with spin and inclination

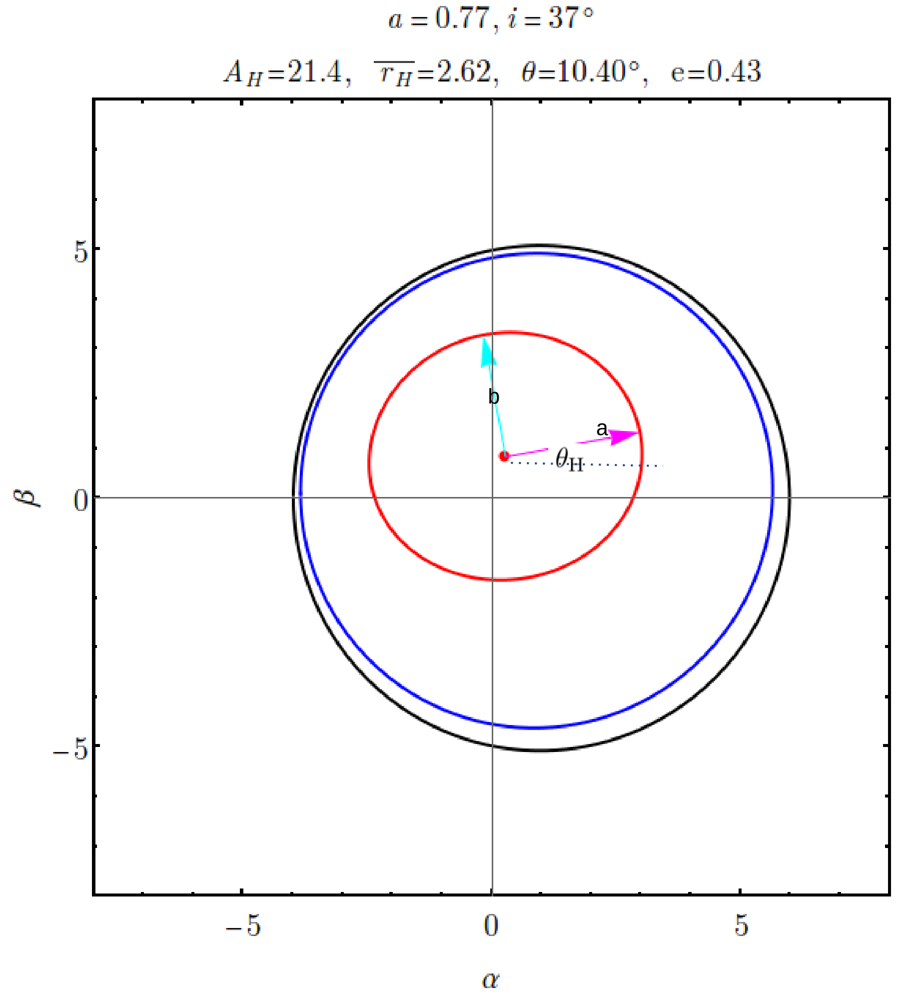
- If observable, it would provide a **second set of constraints** on the metric from observations of the n=1 photon ring (Alex and Avery's talks)

Properties of the lensed horizon image

We characterize the lensed horizon shape with image moments:

- 0th moment: Area
- 1st moment: Centroid
- 2nd moment: Principal axes & orientation

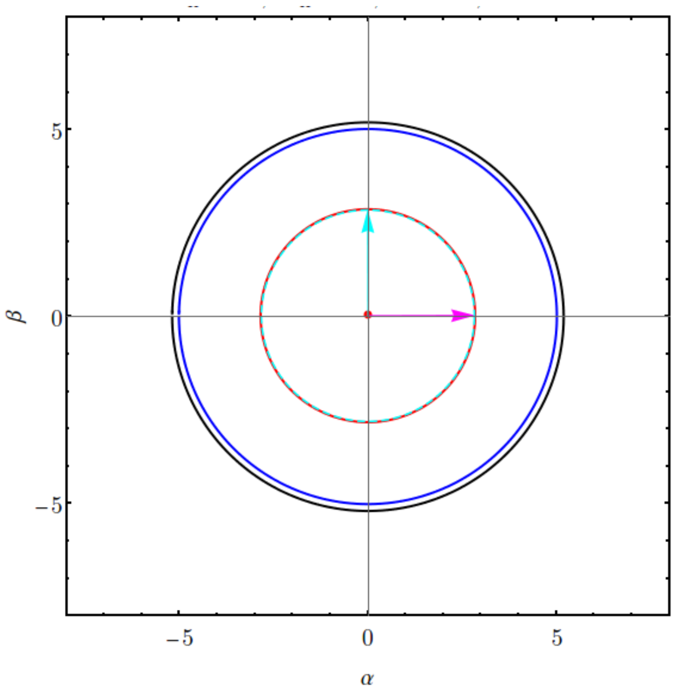
From the 2nd moment we get the mean radius
($\bar{r}_{\rm H}$) , orientation angle $\theta_{\rm H}$), and eccentricity ($e_{\rm H}$)



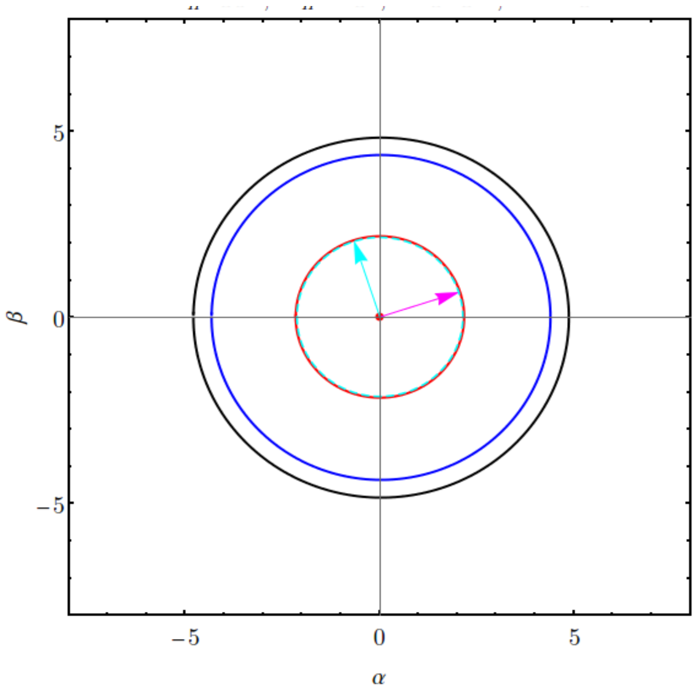
$$\bar{r}_{\rm H} = \sqrt{\frac{a^2 + b^2}{2}} \qquad e_{\rm H} = \sqrt{1 - \frac{b^2}{a^2}}$$

Inner shadow size and shape

At face on inclination: $\rho(a) \approx 2\sqrt{r_+(a)}$

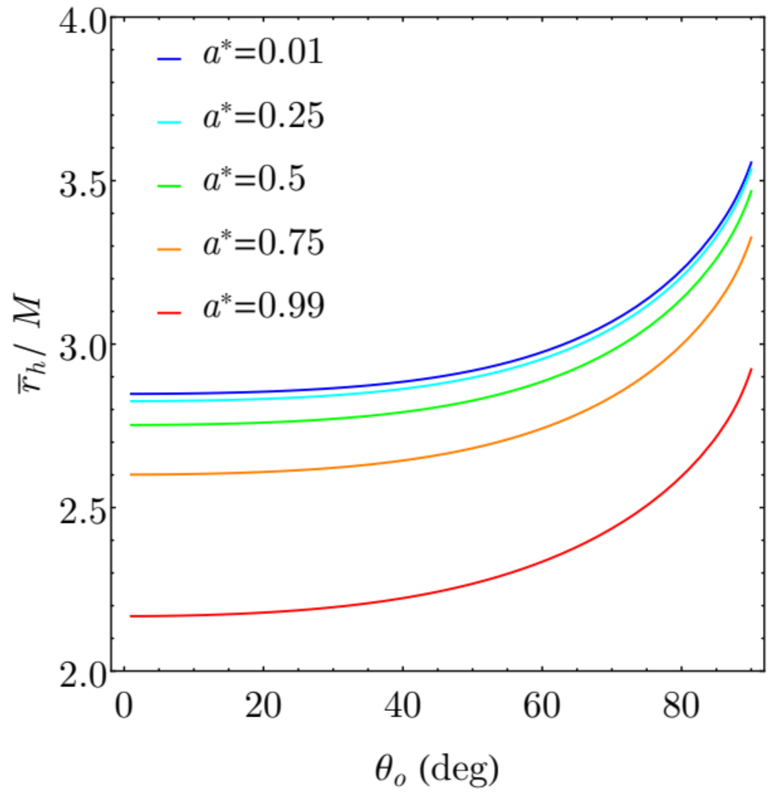


$a = 0, \rho \approx 2\sqrt{2}$

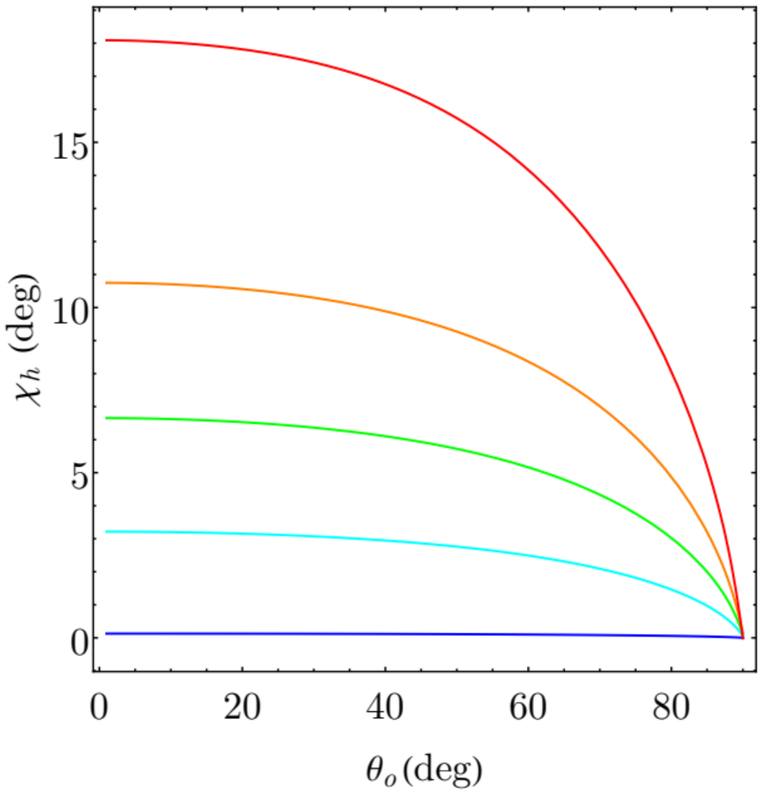


$a = 0.99, \rho \approx 2$

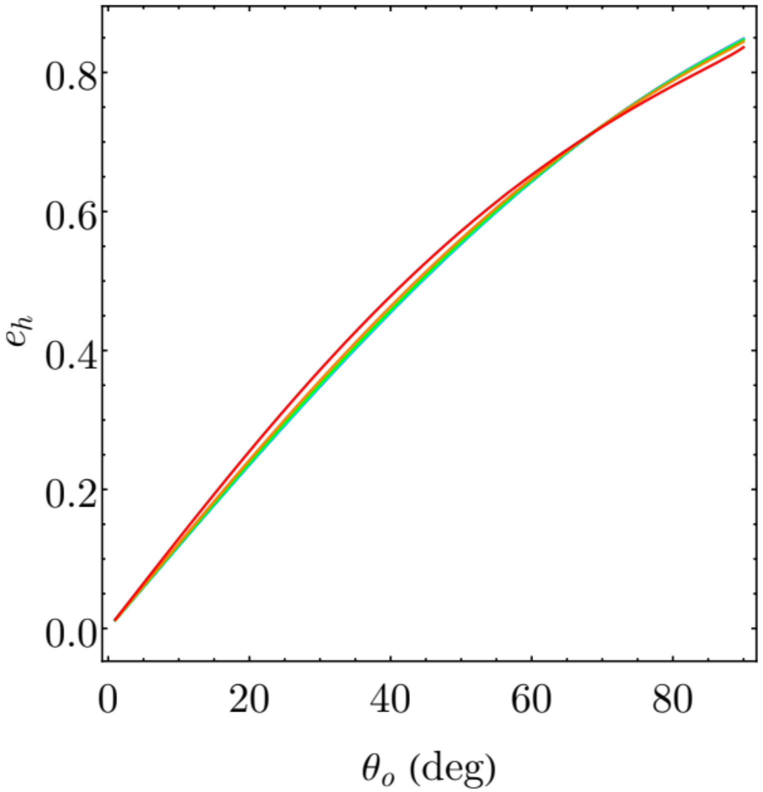
Properties of the lensed horizon image



Radius depends mostly on spin at low inclination



Orientation depends only on spin at low inclinations



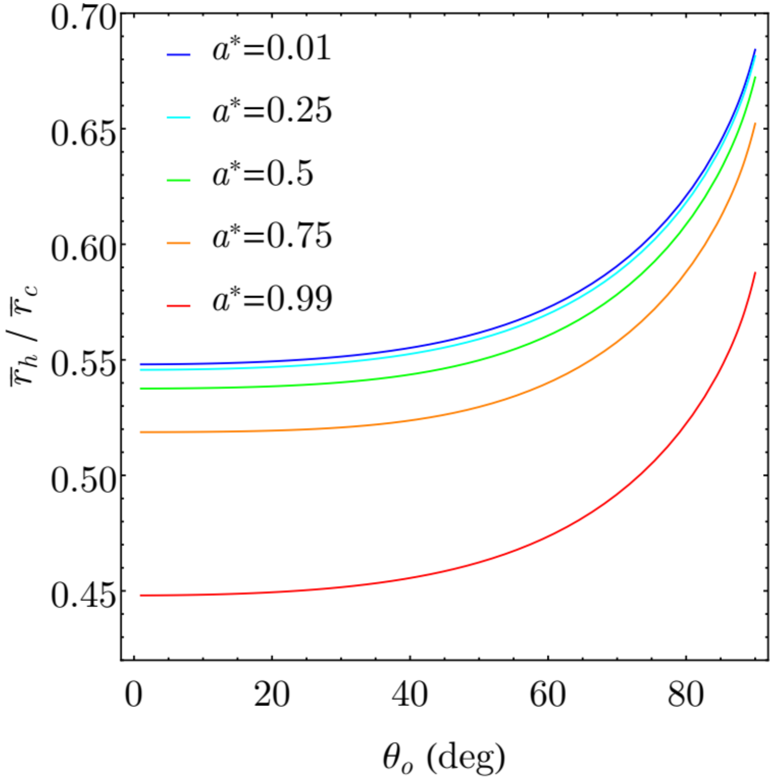
Eccentricity depends ~only on the inclination at all spins

The face-on inner shadow size changes by **~40% from spin 0 to spin 1**, while the shadow/photon ring size changes by only 4% (Johannsen+Psaltis 2010)

Relative centroid and relative radius

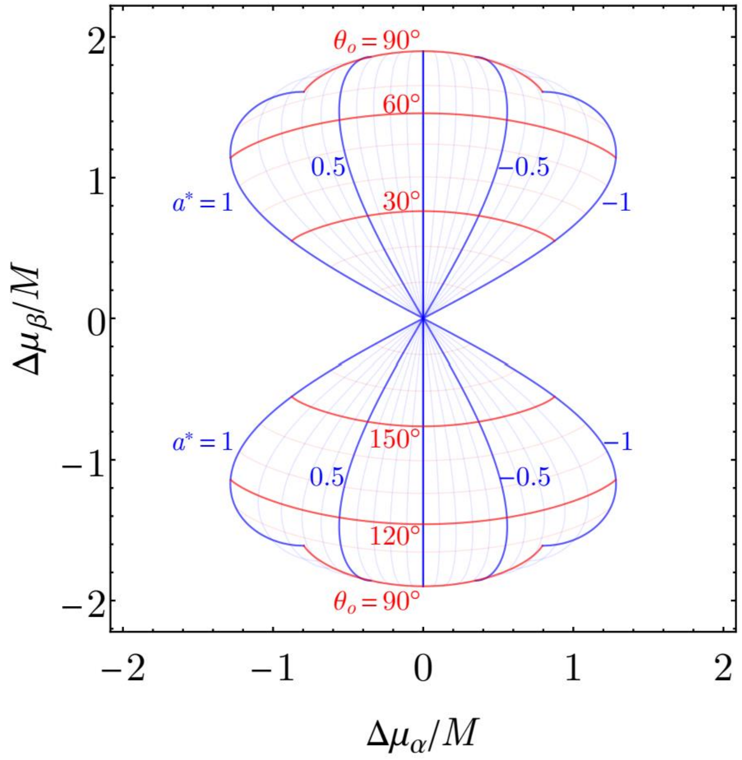
With **two** curves in the image (horizon and photon ring/shadow),
we can measure **relative** offsets and sizes and remove the effect of uncertain mass

Horizon/Critical Curve radius ratio



At low inclination, horizon-to-shadow size
Is **spin-dependent** and decreases from
55% to 45% from a=0 to a=1

Horizon-Critical Curve centroid offset



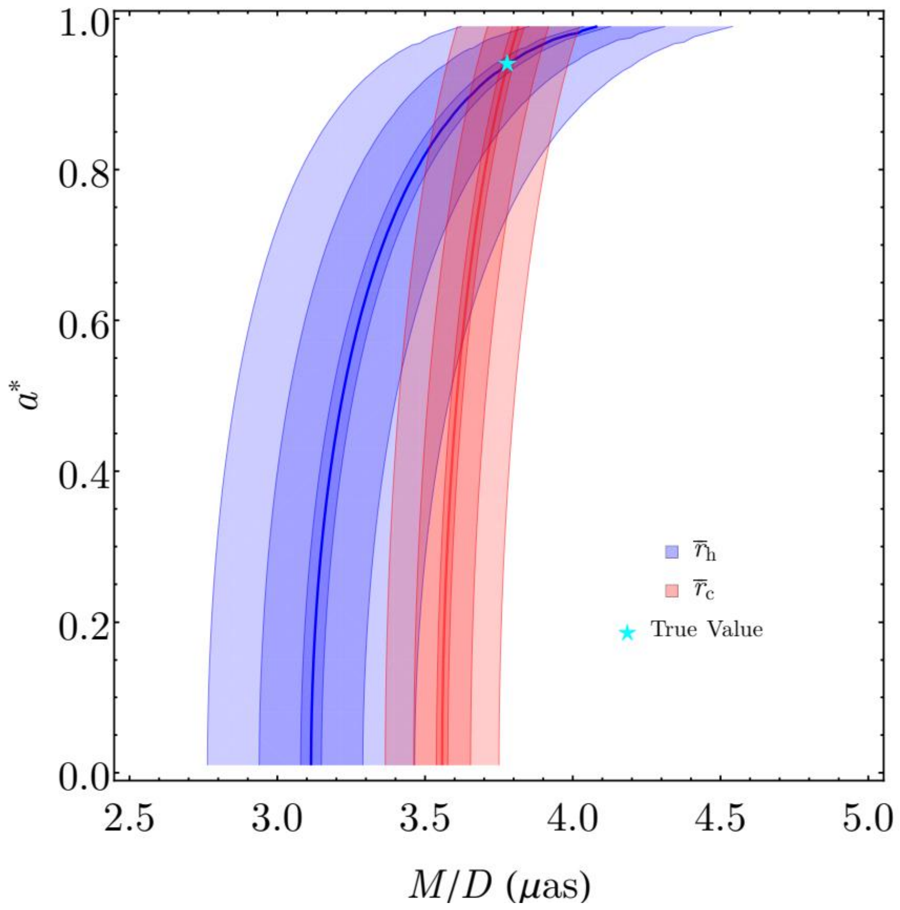
Centroid offset:
angle depends on spin,
magnitude on inclination

$$a \approx -1.64 \arctan\left(\pm_o 0.61 \Delta\alpha/\Delta\beta\right)$$

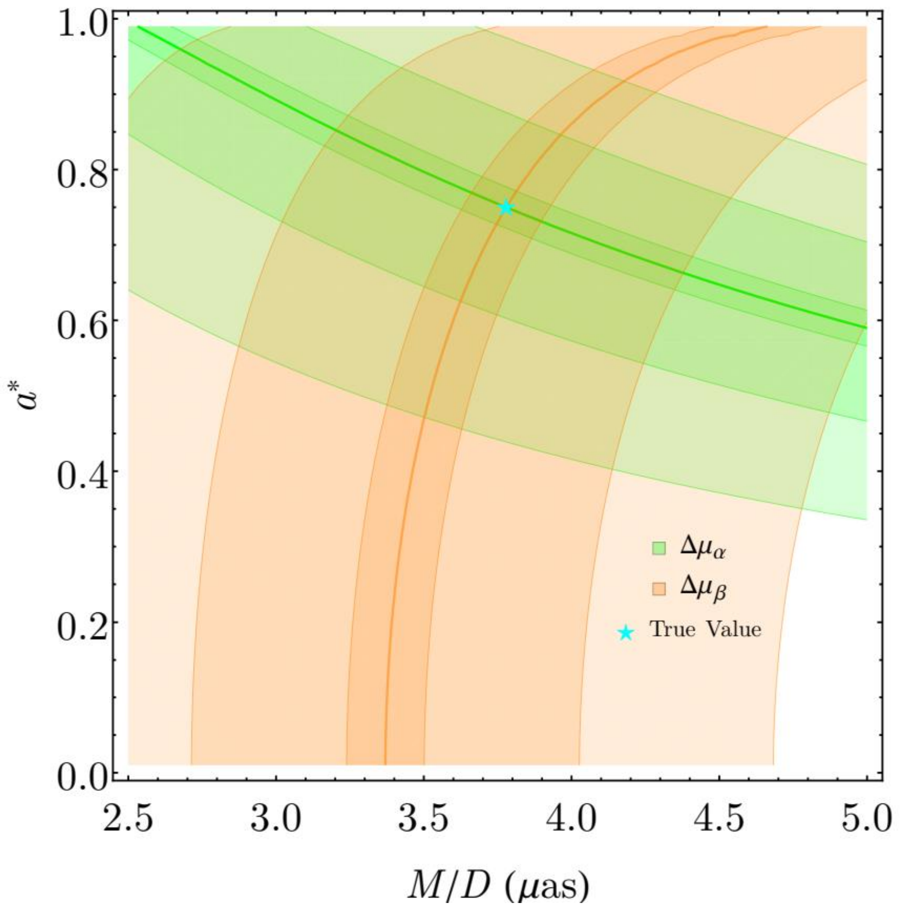
$$\theta_o \approx \pm_{\Delta\beta} 0.42 \sqrt{\Delta\alpha^2 + (\Delta\beta/0.61)^2}.$$

Relative centroid and relative radius: toy example

Measurements of both the inner shadow and photon ring at fixed M87* inclination
Error bands for uncertainties of 0.1, 0.5, 1 uas



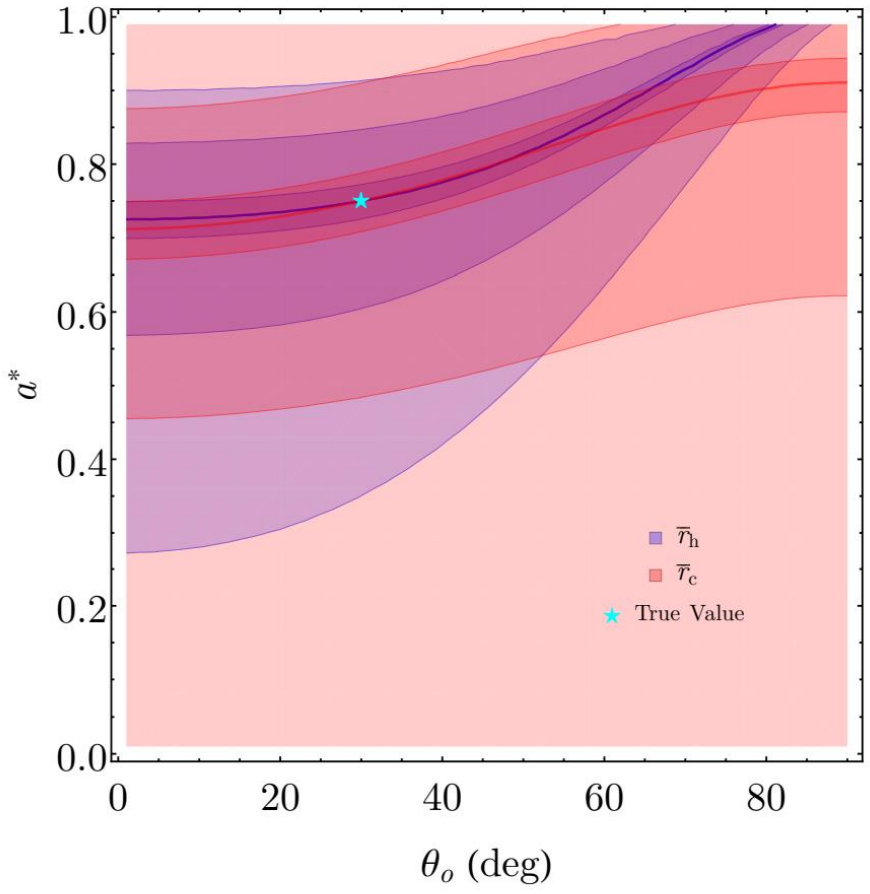
Inner shadow & photon ring sizes



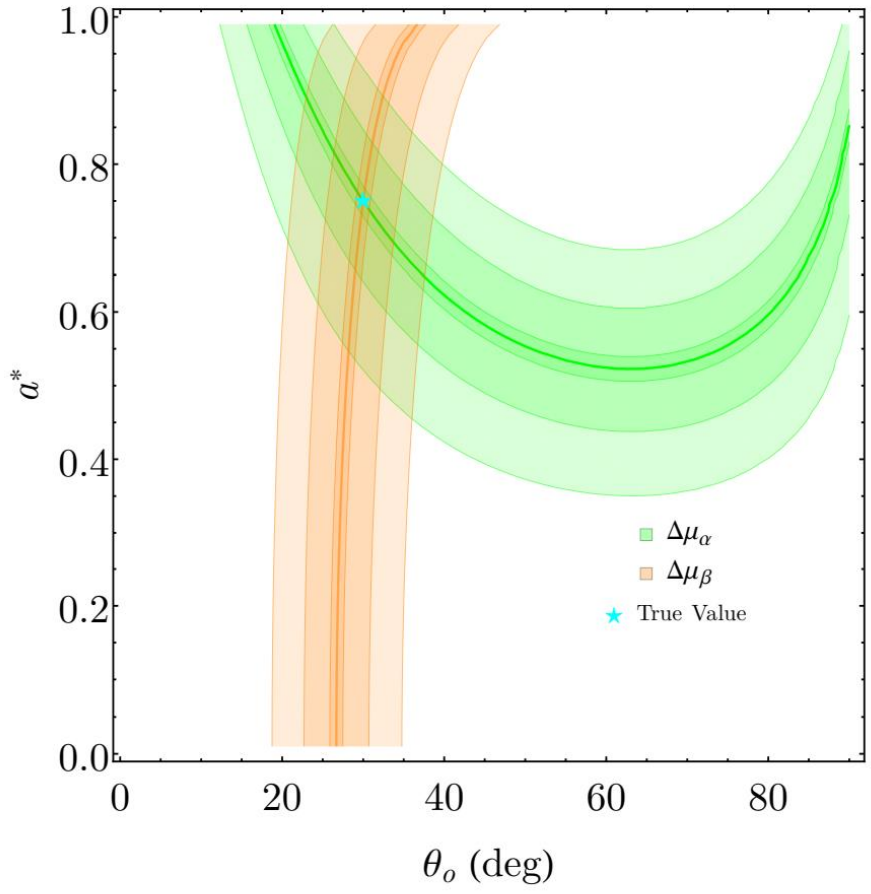
Centroid offset

Relative centroid and relative radius: toy example 2

Measurements of both the inner shadow and photon ring at fixed Sgr A* mass
Error bands for uncertainties of 0.1, 0.5, 1 uas

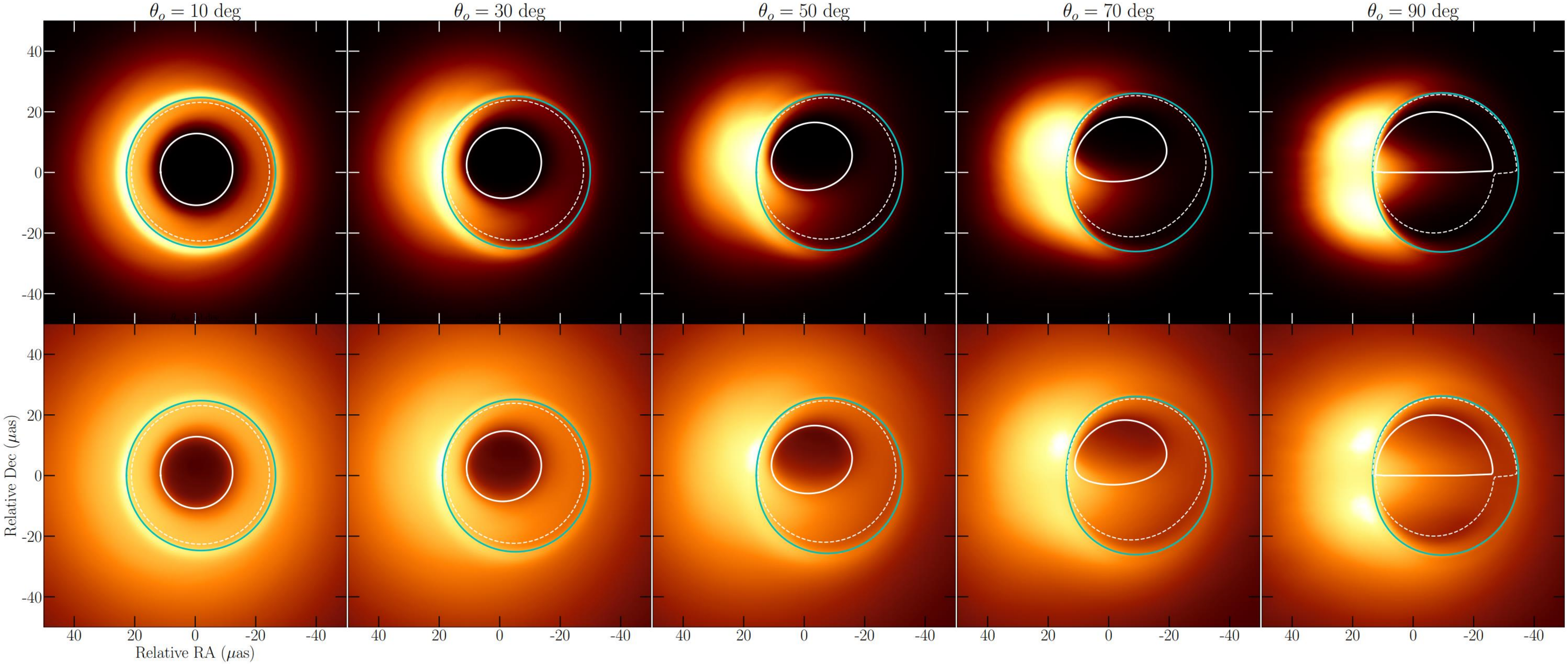


Inner shadow & photon ring sizes



Centroid offset

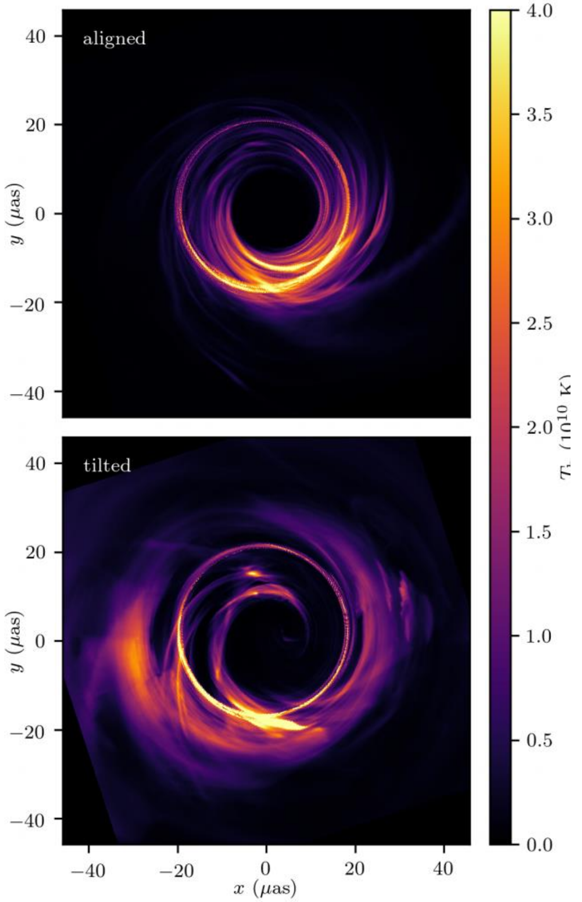
What about disk thickness?
Inner shadow in SANE simulations



Still apparent at low inclination, obscured by thick disk when edge-on

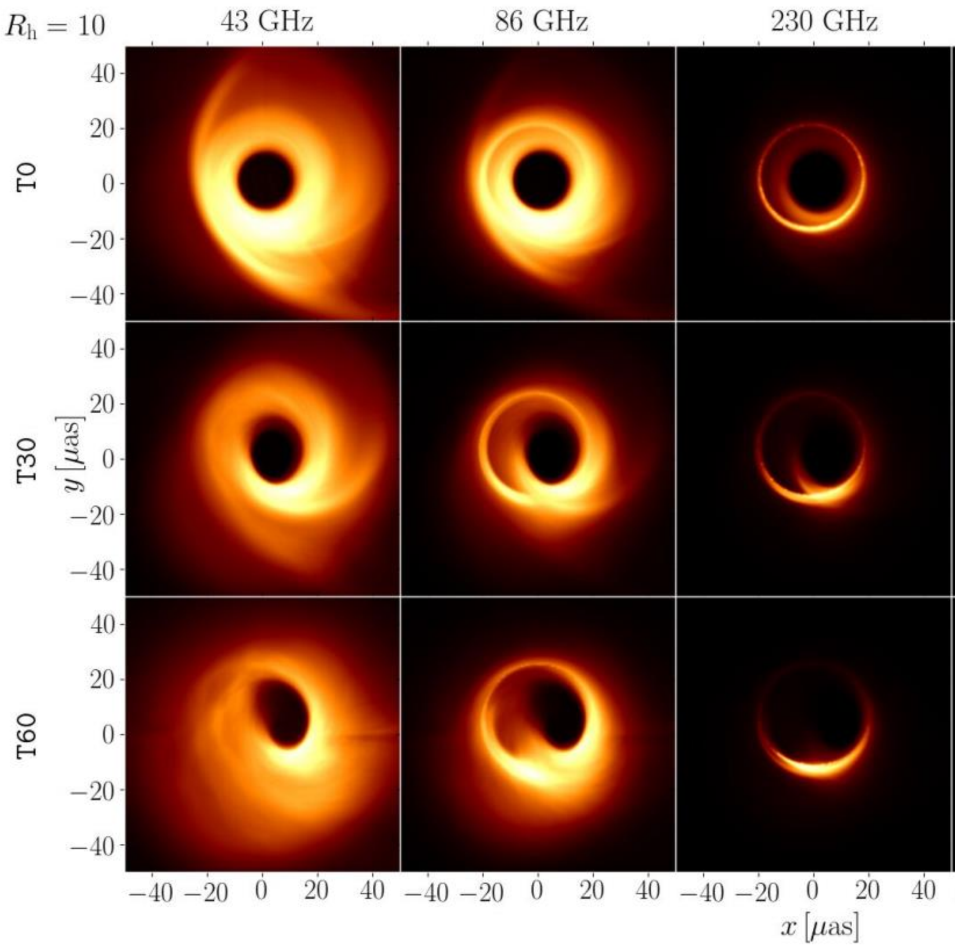
What about disk tilt?

White+ 20 (230 GHz)



Disk tilt can introduce new direct emission features from standing shocks

Chatterjee+20



In these simulations, there is an inner shadow feature with a different size/shape that may originate from the horizon image in the tilted disk plane

Summary

- The lensed (n=0) image of the equatorial event horizon is present in GRMHD simulations and should be observable
- While not ‘universal’ like the photon ring, many GRMHD simulations have the conditions necessary to make this feature observable
- Features of this image (radius, eccentricity, offset from the photon ring) can be used to measure spin and inclination
- The ngEHT will have the dynamic range and resolution necessary to observe this feature, and it could be observable at 86 GHz
- Next steps:
    - Paper on feature properties and appearance in M87 MAD simulations in progress
    - More investigations needed on dependence on simulation parameters!